GENERAL INFORMATION

Instructor: Dr. Rujing Meng
Email: meng@hku.hk
Office: Room 922 K K Leung Building
Phone: 2859-1048
Consultation times: by appointments
Semester: 2
Lecture: Wed 9:30 am -12:20 pm in KK101
Tutor: TBA
Pre-requisites:
  FINA2802/FINA2320 Investments and portfolio analysis
  FINA0301/FINA2322 Derivatives
  MATH1211/MATH2211 Multivariable calculus or MATH2014 Multivariable Calculus and Linear Algebra
Co-requisites:/
Mutually exclusive: MATH2906/MATH3906 Financial calculus

Course Website:
Other important details:

This course provides students with the necessary mathematical techniques used in continuous-time finance. It covers stochastic calculus, partial differential equation and applied probability. After taking this course, one should be able to fully understand no-arbitrage theory, the Black-Scholes equation, risk-neutral probability and martingales. The purpose of this course is to lay down a solid mathematical foundation for students to learn more advanced topics in financial engineering and risk management, such as exotic options, interest rate derivatives and credit risk models.

COURSE OBJECTIVES

1. to fully understand no-arbitrage theory, risk-neutral probability, martingale, and Black-Scholes equation
2. to lay down a solid mathematical foundation for students to learn more advanced topics in financial engineering and risk management, such as exotic options, interest rate derivatives and credit risk models

COURSE LEARNING OUTCOMES

<table>
<thead>
<tr>
<th>Course Learning Outcomes</th>
<th>Aligned Programme Learning Outcomes</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLO1 Understand the concept and properties of a standard Brownian motion. Be able to derive probability distribution of a function of Brownian motion.</td>
<td>Goal 1, Goal 2</td>
</tr>
<tr>
<td>CLO2 Understand stock price model with a lognormal process. Understand the Ito's Lemma. Be able to derive a process for option price by using the Ito's Lemma.</td>
<td>Goal 1, Goal 2</td>
</tr>
<tr>
<td>CLO3 Understand the concept of martingale. Be able to justify whether a process is a martingale or not.</td>
<td>Goal 1, Goal 2</td>
</tr>
</tbody>
</table>
CLO4 Be able to price an option using risk-neutral probability approach.

CLO5 Understand no-arbitrage principle. Be able to derive put-call parity, forward price formula, and the Black-Scholes equation by using the no-arbitrage principle.

CLO6 Understand heat equation and Green's function. Be able to solve the Black-Scholes equation with an arbitrary payoff.

CLO7 Memorize the Black-Scholes formula. Be able to derive Greek letters from the Black-Scholes formula. Understand the asymptotic behavior of the Black-Scholes formula.

**COURSE TEACHING AND LEARNING ACTIVITIES**

<table>
<thead>
<tr>
<th>Course Teaching and Learning Activities</th>
<th>Expected contact hour</th>
<th>Study Load (% of study)</th>
</tr>
</thead>
<tbody>
<tr>
<td>T&amp;L1. Lecture</td>
<td>36 hours</td>
<td>30%</td>
</tr>
<tr>
<td>T&amp;L2. Tutorial</td>
<td>12 hours</td>
<td>10%</td>
</tr>
<tr>
<td>T&amp;L3. Self-study</td>
<td>72 hours</td>
<td>60%</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>120 hours</strong></td>
<td><strong>100%</strong></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Assessment Methods</th>
<th>Brief Description (Optional)</th>
<th>Weight</th>
<th>Aligned Course Learning Outcomes</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1. Assignments</td>
<td></td>
<td>30%</td>
<td>CLO1 – 7</td>
</tr>
<tr>
<td>A2. Exams</td>
<td></td>
<td>60%</td>
<td>CLO1 – 7</td>
</tr>
<tr>
<td>A3. Class/Tutorial participation</td>
<td></td>
<td>10%</td>
<td>CLO1 – 7</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td><strong>100%</strong></td>
<td></td>
</tr>
</tbody>
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**STANDARDS FOR ASSESSMENT**

**Course Grade Descriptors**

- **A+, A, A-** Students demonstrate very good to excellent performance in the defined assessment criteria.
- **B+, B, B-** Students demonstrate good to very good performance in the defined assessment criteria.
- **C+, C, C-** Students demonstrate fair to good performance in the defined assessment criteria.
- **D+, D** Students demonstrate fair performance in the defined assessment criteria.
- **F** Students fail to show understanding of core materials in this course.

**Assessment Rubrics for Each Assessment** (Please provide us the details in a separate file if the space here is not enough)

Assessment for each course component is consistent with the course grade descriptors listed above.

**COURSE CONTENT AND TENTATIVE TEACHING SCHEDULE**

Lecture 1: Introduction and tree approach I
Lecture 2: Tree approach II
Lecture 3: Review of probability
### Lecture 4: Stochastic differential equations
### Lecture 5: Martingale approach I
### Lecture 6: Martingale approach II
### Lecture 7: Partial differential equation approach I
### Lecture 8: Partial differential equation approach II
### Lecture 9: Asymptotic analysis
### Lecture 10: Deriving and hedging with Greeks

### REQUIRED/RECOMMENDED READINGS & ONLINE MATERIALS (e.g. journals, textbooks, website addresses etc.)

#### Reference books

#### MEANS/PROCESSES FOR STUDENT FEEDBACK ON COURSE
- ☐ conducting mid-term survey in additional to SETL around the end of the semester
- ☐ Online response via Moodle site
- ☑ Others: ___ Course Evaluation at the end of the course ___(please specify)

#### COURSE POLICY (e.g. plagiarism, academic honesty, attendance, etc.)

The University Regulations on academic dishonesty will be strictly enforced! Please check the University Statement on plagiarism on the web: [http://www.hku.hk/plagiarism/](http://www.hku.hk/plagiarism/)

#### ADDITIONAL COURSE INFORMATION (e.g. e-learning platforms & materials, penalty for late assignments, etc.)